

Primera serie

(Castellan 12<sup>a</sup> Edición)

18.7)

Datos:

$$r = ? \quad \rho_{\text{serie}} = 1 \text{ g/cm}^3 \quad \theta = 0 \quad \gamma = 73 \times 10^{-3} \text{ N/m}$$

Se desprecia la presión del aire

$$r = \frac{2(\cos \theta) \gamma}{\rho h g} \rightarrow \frac{2(\cos 0^\circ) 73 \times 10^{-3}}{1(30)(9.8)} = 4.9609 \times 10^{-4} \text{ m}$$

18.9)

Datos:

$$r = 0.05 \text{ cm} \quad \gamma = 0.072 \text{ N/m} \quad \Delta P = P$$

$$L = 0.0005 \text{ m}$$

Despreciar la profundidad de inmersión

$$\Delta P = \frac{2\gamma}{r} \rightarrow \frac{2(0.072)}{0.0005} = 288 \text{ pa}$$

18.13)

Datos:

$$T = 20^\circ \text{C} \quad \gamma_{\text{benzene}} = 28.85 \text{ mN/m} \quad \gamma_{\text{agua}} = 72.75 \text{ mN/m}$$

$$\theta = 0^\circ \quad \gamma_{\text{int}} = 35 \text{ mN/m}$$



Determinar

- Trabajo de adhesión entre el agua y el benceno
- Trabajo de cohesión para el benceno y para el agua
- Coefficiente de cohesión para el benceno y el agua

$$a) W_{ad} = \gamma_{agua} + \gamma_{benceno} + \gamma_{int} \rightarrow 72.75 \times 10^{-3} + 28.25 \times 10^{-3} + 35 \times 10^{-3} = 0.1366 \text{ N/m}$$

$$b) W_{coh} = 2\gamma$$

$$A_{agua} = 2(72.75 \times 10^{-3}) = 0.1455 \text{ N/m} \quad \text{Benceno} = 2(28.25 \times 10^{-3}) = 0.05775 \text{ N/m}$$

c)

18.19)

Acido esteárico ( $C_{17}H_{35}(COO)_2$ )  $\rho = 0.85 \text{ gr/cm}^3$   $A = 0.205 \text{ nm}^2$   
 $\hookrightarrow 284 \text{ gr/mol}$   
 $L = ?$

$$\bar{v} = \frac{M}{\rho} = \frac{284 \text{ g/mol}}{0.85 \text{ g/cm}^3} = 334.11 \text{ cm}^3/\text{mol} \left( \frac{1 \text{ m}^3}{10^6 \text{ cm}^3} \right) = 3.3411 \times 10^{-4} \text{ m}^3$$

$$\bar{v}_{molecule} = \frac{\bar{v}}{N_A} = \frac{3.3411 \times 10^{-4} \text{ m}^3/\text{mol}}{6.022 \times 10^{23} \text{ molecules/mol}} = 5.548 \times 10^{-28} \text{ m}^3$$

$$\hookrightarrow \left( \frac{10^9 \text{ nm}^3}{1 \text{ m}^3} \right) = 0.5548 \text{ nm}^3$$

$$\bar{v}_{molecule} = A \cdot L$$

$$L = \frac{\bar{v}_{molecule}}{A_{molecule}} = \frac{0.5548 \text{ nm}^3}{0.205 \text{ nm}^2} = 2.7 \text{ nm}$$



18.25)

a) Acido acetico en agua a  $30^{\circ}\text{C}$   $PM = 60 \text{ g/mol}$

|                                |       |       |       |       |       |       |
|--------------------------------|-------|-------|-------|-------|-------|-------|
| % peso de acido                | 2.475 | 5.001 | 10.01 | 30.09 | 49.96 | 69.91 |
| $\gamma (10^{-3} \text{ N/m})$ | 64.4  | 60.1  | 54.6  | 43.6  | 38.4  | 34.3  |

Graticar  $\gamma$  en funcion de  $\ln m$  y determinar el exceso superficial del acido acetico usando la isoterma de adsorcion de Gibbs

b) Acido propionico en agua a  $25^{\circ}\text{C}$   $PM = 74 \text{ g/mol}$

|                                |      |      |     |      |
|--------------------------------|------|------|-----|------|
| % peso de acido                | 1.91 | 5.34 | 9.8 | 21.7 |
| $\gamma (10^{-3} \text{ N/m})$ | 60   | 49   | 44  | 36   |

$$a) \frac{2.475 \text{ g}}{60 \text{ g/mol}} = 4.125 \times 10^{-3} \text{ mol} \quad \frac{5.001 \text{ g}}{60 \text{ g/mol}} = 0.08335 \text{ mol}$$

$$\frac{10.01 \text{ g}}{60 \text{ g/mol}} = 0.167 \text{ mol} \quad \frac{30.09 \text{ g}}{60 \text{ g/mol}} = 0.5015 \text{ mol}$$

$$\frac{49.96 \text{ g}}{60 \text{ g/mol}} = 0.832 \text{ mol} \quad \frac{69.91 \text{ g}}{60 \text{ g/mol}} = 1.165 \text{ mol}$$

$$4.125 \times 10^{-3} - \frac{97.525 \text{ g}}{1000 \text{ g}} = 0.0423 \quad 0.08335 - \frac{94.999 \text{ g}}{1000 \text{ g}} = 0.877$$

$$0.167 - \frac{89.999 \text{ g}}{1000 \text{ g}} = 1.855 \quad 0.5015 - \frac{69.91 \text{ g}}{1000 \text{ g}} = 7.173$$

$$0.832 - \frac{50.04 \text{ g}}{1000 \text{ g}} = 16.626 \quad 1.165 - \frac{30.09 \text{ g}}{1000 \text{ g}} = 38.717$$



| $m(C_2)$ | $\ln x$ | $\gamma (10^{-3} N/m)$ |
|----------|---------|------------------------|
| 0.0422   | -3.165  | 64.4                   |
| 0.277    | -0.131  | 60.1                   |
| 1.255    | 0.61    | 54.6                   |
| 7.173    | 1.97    | 43.6                   |
| 16.626   | 2.81    | 38.4                   |
| 32.717   | 3.626   | 34.3                   |

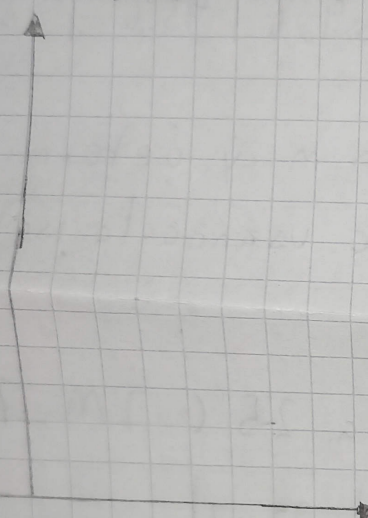
$$A = 53.759$$

$$B = -4.747 \times 10^{-3} N/m$$

$$r = -0.942$$

$$\Gamma_2 = \frac{-(-4.747 \times 10^{-3})}{(2.314)(303.15)}$$

$$= 1.223 \mu mol/m^2$$



b)

$$\frac{1.91g}{74g/mol} = 0.0258 mol \quad \frac{5.241g}{74g/mol} = 0.0789 mol$$

$$\frac{9.2g}{74g/mol} = 0.1324 mol \quad \frac{21.7g}{74g/mol} = 0.2932 mol$$

$$0.0258 - \frac{92.04g}{1000g} = 0.263 \quad 0.0789 - \frac{94.16g}{1000g} = 0.8379$$

$$0.1324 - \frac{90.2g}{1000g} = 1.4678 \quad 0.2932 - \frac{78.3g}{1000g} = 3.7445$$

| $m(C_2)$ | $\ln x$ | $\gamma (10^{-3} N/m)$ |
|----------|---------|------------------------|
| 0.263    | -1.3356 | 6.0                    |
| 0.8379   | -0.1786 | 4.9                    |
| 1.4678   | 0.3837  | 4.4                    |
| 3.7445   | 1.3202  | 3.6                    |

$$A = 47.6858$$

$$B = -9.0475$$

$$r = -0.9996$$

$$\Gamma_2 = \frac{-(-9.0475 \times 10^{-3})}{(2.3145)(298.15)}$$

$$= 3.6497 \mu mol/m^2$$



Atkins (3<sup>ra</sup> edición)

A7.9)

$$T = 20^{\circ}\text{C} \quad M = 154 \text{ g/mol}$$

$$\gamma_{\text{cccl}_4} = 0.027 \text{ N m}^{-1}$$

$$\rho = 1.6 \text{ g/cm}^3$$

$$P^{\circ} = 87.05 \text{ Torr} \quad P = 87.95 \text{ Torr}$$

$$\gamma = \frac{2\gamma\bar{V}}{RT \ln(P/P^{\circ})} \quad \bar{V} = \frac{M}{\rho} = \frac{154 \text{ g/mol}}{1.6 \text{ g/cm}^3} = 96.25 \text{ cm}^3 \times \frac{1 \text{ m}^3}{10^6 \text{ cm}^3} = 9.625 \times 10^{-5} \text{ m}^3$$

$$r = \frac{2(0.027 \text{ N m}^{-1})(9.625 \times 10^{-5} \text{ m}^3)}{(8.314 \frac{\text{J}}{\text{mol K}})(293.15 \text{ K}) \ln(\frac{87.95 \text{ Torr}}{87.05 \text{ Torr}})} = 2.07 \times 10^{-7} \text{ m}$$

A7.10)

$$P_{\text{int}} = ? \quad P_{\text{ext}} = 740 \text{ Torr} \quad r = 0.125 \text{ mm} \quad \gamma = 5.7 \times 10^{-2} \text{ N/m}$$

$L = 0.00125 \text{ m}$

Calcular presión interna de la burbuja

$$\Delta P = \frac{2\gamma}{r} \rightarrow P_{\text{int}} - P_{\text{ext}} = \frac{2\gamma}{r} \rightarrow P_{\text{int}} = \frac{2\gamma}{r} + P_{\text{ext}}$$

$$P_{\text{int}} = \left( \frac{2(5.7 \times 10^{-2} \text{ N/m})}{2.25 \times 10^{-4} \text{ m}} \right) + 740 \text{ Torr} = 1652 \text{ Torr}$$



7.39) En cuanto cambia la presión de vapor del benceno cuando este se dispersa en forma de pequeñas gotas de radio a)  $10 \mu\text{m}$ , b)  $0.10 \mu\text{m}$  a  $25^\circ\text{C}$ ?

7.41)

$$A_{\text{succ}} \quad h = \frac{2\gamma}{\rho r g}$$

$$\gamma = 7.28 \times 10^{-2} \text{ N/m (a } 20^\circ\text{C)} \quad \gamma = 5.8 \times 10^{-2} \text{ N/m (a } 100^\circ\text{C)}$$

$$\rho = 0.998 \text{ g/cm}^3 \rightarrow 998 \text{ kg/m}^3 \quad \rho = 0.958 \text{ g/cm}^3 \rightarrow 958 \text{ kg/m}^3$$

Calcular elevación en tubos de a)  $1 \text{ mm}$  b)  $0.1 \text{ mm}$  de radio  
 $\hookrightarrow 0.001 \text{ m} \quad \hookrightarrow 0.0001 \text{ m}$

$$\frac{2(5.8 \times 10^{-2} \frac{\text{kg} \cdot \text{m}}{\text{s}^2})}{998 \frac{\text{kg}}{\text{m}^3} (0.001 \text{ m}) (9.81 \frac{\text{m}}{\text{s}^2})} = 0.0118 \text{ m} \quad \left( \frac{2(5.8 \times 10^{-2} \frac{\text{kg} \cdot \text{m}}{\text{s}^2})}{958 \frac{\text{kg}}{\text{m}^3} (0.001 \text{ m}) (9.81 \frac{\text{m}}{\text{s}^2})} \right)$$

$$\frac{2(5.8 \times 10^{-2} \frac{\text{kg} \cdot \text{m}}{\text{s}^2})}{998 \frac{\text{kg}}{\text{m}^3} (0.0001 \text{ m}) (9.81 \frac{\text{m}}{\text{s}^2})} = 0.1124 \text{ m}$$

$$= 0.0123 \text{ m}$$

$$\frac{2(5.8 \times 10^{-2} \frac{\text{kg} \cdot \text{m}}{\text{s}^2})}{958 \frac{\text{kg}}{\text{m}^3} (0.0001 \text{ m}) (9.81 \frac{\text{m}}{\text{s}^2})}$$

$$= 0.1234 \text{ m}$$

$20^\circ\text{C}$

$25^\circ\text{C}$



Laidler (1<sup>ra</sup> edición)

18.17)

$$\gamma = 7.27 \times 10^{-2} \text{ N/m} \quad \rho = 0.998 \text{ g/cm}^3 \quad \theta = 0^\circ \quad g = 9.81 \text{ m/s}^2$$

$\hookrightarrow 998 \text{ kg/m}^3$

- a) Calcular elevación del agua en capilares de 1 mm de radio  
b) Calcular elevación del agua en capilares de  $10^{-3}$  cm radio

Para a):

$$h = \frac{2\gamma \cos \theta}{\rho g r} = \frac{2(7.27 \times 10^{-2})(\cos 0^\circ)}{(998)(9.81)(0.001)} = 0.1485 \text{ m}$$

Para b):

$$\begin{aligned} \hookrightarrow 1.485 \times 10^{-2} \text{ m} \\ \hookrightarrow 1.485 \text{ cm} \end{aligned}$$

$$\frac{2(7.27 \times 10^{-2})(\cos 0^\circ)}{998(9.81)(1 \times 10^{-5})} = 1.4851 \text{ m}$$

18.21)

$$h_1 = 1.5 \text{ cm} \quad \theta = 0^\circ \quad \gamma_2 = \frac{1}{2} \gamma_1 \quad \rho_2 = \frac{1}{2} \rho_1 \quad g = 9.81 \text{ m/s}^2$$

$$h_2 = ?$$



18.25)

$$A = \frac{1}{2} \text{ acre} \rightarrow 1 \text{ acre} = 4840 \text{ yd}^2 \rightarrow 1 \text{ yard} = 0.915 \text{ m}$$

$$V = 1 \text{ cm}^3 \text{ espesor} = ?$$

$$4840(0.915)^2 = 4052 \text{ m}^2 \quad ; \quad \frac{1}{2} \text{ acre} = 2026 \text{ m}^2$$

$$\frac{1 \times 10^{-6} \text{ m}^3}{2026 \text{ m}^2} = 4.9358 \times 10^{-10} \text{ m}$$

$$1 \text{ cm}^3 = 1 \times 10^{-6} \text{ m}^3$$

18.26)

$$T = 15^\circ \text{C}$$

|   |     |      |     |      |      |        |
|---|-----|------|-----|------|------|--------|
| $A = \text{cm}^2 \text{ } \mu\text{s}^{-1}$ | 5.1 | 28.2 | 607 | 1070 | 2200 | 11,000 |
| $\delta = 10^{-3} \text{ N/m}$              | 30  | 0.3  | 0.2 | 0.1  | 0.05 | 0.01   |

Estimar el peso molecular y el area por molecula cuando la pelicula este totalmente comprimida

$$1.11 \times 10^4 \text{ Nm/kg} = (\text{J/kg})$$

$$8.3145(288.15) = 2,395.823 \text{ J/mol}$$

$$PM = \frac{2,395.823 \text{ J/mol}}{1.11 \times 10^4 \text{ J/kg}} = 0.2158 \text{ kg/mol} \rightarrow 215.8 \text{ g/mol}$$

$$1 \mu\text{s} = \frac{6.022 \times 10^{23} (10^{-6})}{2.16} = 2.7879 \times 10^{15} \text{ moleculas}$$



$$A_{\text{molecula}} = \frac{5.7 \text{ cm}^2}{2.7879 \times 10^{15}} = 2.0445 \times 10^{-15} \text{ cm}^2/\text{molecula}$$

$$= 0.2044 \text{ nm}^2/\text{molecula}$$

$$18.18) \ln \frac{P}{P_0} = \frac{2\gamma \bar{v}}{rRT}$$

$P$  = Presión de vapor de las gotitas

$P_0$  = Presión de vapor en sup. plana

$r$  = radio de las gotas

$$m = 10^{-12} \text{ g}$$

$$\gamma = 7.27 \times 10^{-2} \text{ Nm}^{-1}$$

$$\rho = 0.998 \text{ g/cm}^3$$

$$M = 18 \text{ g/mol}$$

$$T = 20^\circ \text{C}$$

$$\rho = \frac{m}{V_{\text{gota}}}$$

$$V_{\text{gota}} = \frac{m}{\rho} = \frac{10^{-12} \text{ g}}{0.998 \text{ g/cm}^3} = 1.002 \times 10^{-12} \text{ cm}^3$$

$$V_{\text{gota}} = \frac{4}{3} \pi r^3$$

$$r = \sqrt[3]{\frac{3 V_{\text{gota}}}{4 \pi}} \rightarrow \sqrt[3]{\frac{3(1.002 \times 10^{-12} \text{ cm}^3)}{4 \pi}}$$

$$r = 6.208 \times 10^{-5} \text{ cm} \left( \frac{1 \text{ m}}{100 \text{ cm}} \right) = 6.208 \times 10^{-7} \text{ m}$$

$$\rho = \frac{M}{\bar{v}} \rightarrow \bar{v} = \frac{M}{\rho} = \frac{18 \text{ g/mol}}{0.998 \text{ g/cm}^3}$$

$$L > 0.204 \frac{\text{cm}^2}{\text{mol}} \left( \frac{1 \text{ m}^3}{10^6 \text{ cm}^3} \right) = 1.804 \times 10^{-5} \text{ m}^3/\text{mol}$$

$$\frac{P}{P_0} = \exp \left[ \frac{2\gamma \bar{v}}{rRT} \right]$$

$$\frac{2\gamma \bar{v}}{rRT} = \frac{2(7.27 \times 10^{-2} \text{ Nm}^{-1})(1.804 \times 10^{-5} \text{ m}^3/\text{mol})}{(6.208 \times 10^{-7} \text{ m})(8.314 \frac{\text{J}}{\text{mol K}})(293.15 \text{ K})}$$

$$L > 1.7345 \times 10^{-3}$$